

Estimating Determinants of Multiple Treatment Episodes for Substance Abusers

Allen C. Goodman,^{1*} Janet R. Hankin,² David E. Kalist,³ Yingwei Peng⁴ and Stephen J. Spurr¹

¹Department of Economics, Wayne State University, Detroit MI 48202, USA

²Department of Sociology, Wayne State University, Detroit, MI 48202, USA

³Department of Economics, Oakland University, Rochester MI 48309, USA

⁴Department of Mathematics and Statistics, Memorial University of Newfoundland, St. John's Newfoundland, Canada

Abstract

Background: Health services researchers have increasingly used hazard functions to examine illness or treatment episode lengths and related treatment utilization and treatment costs. There has been little systematic hazard analysis, however, of mental health/substance abuse (MH/SA) treatment episodes.

Aims of the Study: This article uses proportional hazard functions to characterize multiple treatment episodes for a sample of insured clients with at least one alcohol or drug treatment diagnosis over a three-year period. It addresses the lengths and timing of treatment episodes, and the relationships of episode lengths to the types and locations of earlier episodes. It also identifies a problem that occurs when a portion of the sample observations is "possibly censored." Failure to account for sample censoring will generate biased hazard function estimates, but treating all potentially censored observations as censored will overcompensate for the censoring bias.

Methods: Using insurance claims data, the analysis defines health care treatment episodes as all events that follow the initial event irrespective of diagnosis, so long as the events are not separated by more than 30 days. The distribution of observations ranges from 1 day to 3 years, and individuals have up to 10 episodes. Due to the data collection process, observations may be right censored if the episode is either ongoing at the time that data collection starts, or when the data collection effort ends. The Andersen-Gill (AG) and Wei-Lin-Weissfeld (WLW) estimation methods are used to address relationships among individuals' multiple episodes. These methods are then augmented by a probit censoring model that estimates censoring probability and adjusts estimated behavioral coefficients and medians accordingly.

Results: Five sets of variables explain episode duration: (i) *individual*; (ii) *insurance*; (iii) *employer*; (iv) *binary*, indicating episode diagnosis, location, and sequence; and (v) *linkage*, relating current diagnoses to previous diagnoses in a sequence. Sociodemographic variables such as age or gender have impacts at both the individual and at the firm level. Coinsurance rates and deductibles also have impacts at the individual and the firm levels. Binary variables indicate that surgical/outpatient episodes were the shortest, and psychiatric/outpatient episodes were the longest. Linkage variables reveal significant impacts

of prior alcoholism, drug, and psychiatric episodes on the lengths of subsequent episodes.

Discussion: Health care treatment episodes are linked to each other both by diagnosis and by treatment location. Both the AG and the WLW models have merit for treating multiple episodes. The AG model permits more flexibility in estimating hazards, and allows researchers to model impacts of prior diagnoses on future episodes. The WLW model provides a convenient way to examine impacts of sociodemographic variables across episodes. It also provides efficient pooled estimates of coefficients and their standard errors.

Limitations: The insurance claims data set covers 1989 through 1991, predating current managed care plans. It cannot identify untreated substance abusers, nor can it identify those with out-of-plan use. It provides treatment information only if services are covered by the insurance plan and are defined with a substance abuse diagnosis code. Like medical records, insurance claims will not specify substance abuse treatment received within the context of other health care (and thus identified by a non-substance abuse diagnosis code) or community services

Implications for Policy and Research: This article characterizes multiple health treatment episodes for a sample of insured clients with at least one alcohol or drug treatment diagnosis within a three-year period. We identify both individual and employer effects on episode length. We find that episode lengths vary by the diagnosis type, and that the lengths (and by inference cost and utilization) may depend on the treatments that occurred in previous episodes. We also recognize that health care or illness episodes may be ongoing at times of health care events prior to the ends of data collection periods, leading to uncertain episode lengths. Corresponding estimates of costs or utilization are also uncertain. We provide a method that adjusts the episode lengths according to the probability of censoring.

Received 8 July 2001; accepted 10 October 2001

Introduction

Health services researchers have increasingly used hazard functions to examine illness or treatment episode lengths, and related treatment utilization and treatment costs. This article addresses the lengths and timing of multiple episodes within a three-year observation window. It also addresses the relationships of individual episodes' lengths to the types and locations of previous episodes and it considers a class of problems in which a portion of the sample observations is "possibly censored." Although failure to account for sample

*Correspondence to: Allen C. Goodman, Department of Economics, Wayne State University, 2145 FAB, 656 W. Kirby, Detroit, MI 48202 USA
Phone +1-313-577 3235
Fax +1-313-577 0149
Email: allen.goodman@wayne.edu

Sources of Funding: The research is partially supported by Grant DA10828 from the National Institute on Drug Abuse (NIDA), and from a grant from the Blue Cross Blue Shield Foundation. The data analyzed were purchased from MEDSTAT© Systems, Inc under NIDA grant DA08711.

censoring will generate biased estimates in hazard function analysis, treating *all* potentially censored observations as censored will overcompensate for the censoring bias.

We apply the analysis to the lengths of health care treatment episodes. We show how various classes of individual, employer, diagnosis and sequence characteristics affect episode length. We then use resampling techniques to provide unbiased estimates for medians. When applied to a health insurance claims database, the estimator provides larger medians than those calculated with no censoring adjustments, but smaller than those that assume that all potentially censored observations are, in fact, censored.

Methods

Treatment Episodes

Episode definition and analysis have provided an intuitive yet elusive framework for analyzing health services utilization and costs. For many conditions, costs and utilization begin when episodes begin, and end when the episodes end, irrespective of the calendar. It is important to understand episode lengths and patterns in order to determine personnel and facility needs and health care costs, and to assure health care quality. Screening procedures or health care treatments that can prevent or shorten episodes may have substantive impacts on health care use and health care costs.

Unfortunately, episode definition may be quite arbitrary and difficult to implement. An illness episode may begin some time before treatment is sought, and end some time after treatment is finished. Treatment episodes may span numerous treatment locations (providers' offices, clinics, and/or hospitals), leading to problems in tracing the subjects and in collecting the data. Definitions of either illness or treatment episodes are often quite arbitrary because different studies may define episodes by treatment locations (inpatient or outpatient), mental health/substance abuse (MH/SA) or non-MH/SA diagnoses, or arbitrary time separations, typically 30 or 60 days.

Our analysis focuses on *treatment* rather than illness episodes. The distinction is important because illness episodes, especially for chronic illnesses with vague symptoms and imprecise beginning dates, may be difficult to define in terms of start, duration, and conclusion. Treatment episodes, in contrast, can be defined with specific beginning and ending treatment events.

Measuring episode length is of more than academic significance, because it can improve cost estimates for substance abuse treatment. Frank and McGuire characterize the MH/SA treatment cost estimates as among the "most variable" components of the entire 1993-94 debate initiated by the proposed Health Security Act.¹ Mechanic, Schlesinger and McAlpine implicitly frame the issue of episodes in the context of managed care, noting that those with drug or alcohol consumption may struggle over an extended period, often requiring a series of different forms of treatment or continuing aftercare and supportive services.²

There are three major issues in constructing and analyzing health treatment episodes: (i) which services to include; (ii) whether episodes should be limited to single diagnoses or

include multiple diagnoses; and, (iii) when one episode ends and another begins.

There is a lack of consensus regarding treatment norms concerning which services to include. Some studies refer only to episodes of inpatient care, but this approach fails to recognize the importance of outpatient visits before and after the hospitalization.³⁻⁵ We choose a more inclusive method that uses both inpatient and outpatient events to define a treatment episode.⁶

The second issue is whether an episode should be defined with only one diagnosis or a set of related diagnoses. Solon (1967) suggests that it may be important whether conditions are medically managed separately or with a coordinated plan. A series of RAND studies refer to a "medical problem" as the basis for grouping episode expenses.⁷⁻¹² Thus services found to be related to the same problem are grouped into one episode.

The time interval between the end of one episode and the beginning of another is a third issue, requiring a definition of the episode's beginning and end. Typically, with claims data or medical records, the treatment episode begins with a condition's first diagnosis and ends when the condition is no longer being treated. It is possible to define an episode's start as the most recent patient/provider encounter prior to the diagnosis of a specific condition. An alternative is to define the episode's beginning as the point at which a treatment protocol is initiated.¹³ The episode's end may also reflect exhaustion of insurance benefits.

The interval between episodes depends on the medical condition being considered and is often determined by clinical consensus. Moscovice uses physician estimates to determine the expected time frame for several acute conditions.¹⁴ The episode begins with the first medical event within the time frame and ends with the last. If a second event occurs, the reason for the visit is used to determine if the treatment represents a new episode or part of the last one. Cave refers to a "reasonable" time to consider follow-up visits as part of the same episode.¹⁵ For example, a gap of 20 days between treatment events for the same diagnosis may represent a single treatment episode, while a gap of 35 days between two events may signal the beginning of a new treatment episode.

Chronic conditions such as psychiatric and substance abuse problems present additional problems in distinguishing one episode from the next. Typically, arbitrary intervals during which there was no treatment are used to separate episodes of care. Kessler et al. use 8 weeks between psychiatric treatments to define different episodes, but this definition has not been rigorously analyzed in other settings.¹⁶ Intervals of 8 weeks, 2 months, or 60 days have commonly delineated different episodes in both psychiatric and other types of health care literature.^{6,17-19} Berndt, Busch, and Frank also use an 8-week period without treatment to define new episodes, but note that alternative definitions such as 6 or 12 week intervals leave the results "essentially unaffected."²⁰

We define episodes based on a 30-day break point, suggested by technical consultant Thomas McLellan. We include all events that follow an episode's initiation irrespective of diagnosis, so long as they are not separated by more than 30 days. Several major agencies use the proportion of people

discharged from a treatment setting (particularly inpatient) and readmitted within 30 days as a key clinical “performance indicator”. Most of these agencies also wish to see patients transferred from more intensive care (inpatient, intensive outpatient) to less intensive care settings (outpatient), again within 30 days of discharge. These include the National Committee on Quality Assurance (NCQA), American Managed Behavioral Health Association (AMBHA), and Substance Abuse and Mental Health Services Administration (SAMHSA).

This cut-off reflects the premise that maintaining people in treatment for long time periods by “transitioning” them through a “continuum of care” (hospital, residential, intensive outpatient/halfway house, outpatient) leads to the best outcomes. Thus the patient's receiving repeated treatments at intervals within 30 days indicates that the episode is not yet completed.

Defining Episodes with Hazard Functions

We begin our analyses of episode lengths by assuming that episodes are seen in their entirety (i.e. there is no censoring). Suppose that a researcher has collected data on subjects who may have had a treatment for a specific illness. The goal is to characterize the length T of the treatment episode. The cumulative distribution of T is:

$$F(t) = \int_0^t f(s)ds = Prob(T \leq t), \quad (1)$$

where s represents the episode length, and $f(s)$ is a probability density function (PDF). The survival function $S(t)$ is the probability that an episode will still be in progress at length t :

$$S(t) = 1 - F(t) = Prob(T > t), \quad (2)$$

To address a particular episode length, and the probability that it will end in the next interval Δt , define *hazard rate* $\lambda(t) = f(t)/S(t)$ as the instantaneous rate of episode termination for an episode still in progress at length t .

Both the hazard function and the survival function from equation (2) provide important episode-related information. The hazard function indicates whether it is more or less likely that episodes will end as duration increases. An increasing hazard (more likely to end) thus means a shorter episode, and a decreasing hazard means a longer one.

The survival function provides statistical insight into the definition of episode length. Recall that function $S(t)$ varies between 1 (the shortest episode) and 0 (the longest episode). The median occurs at $S(t) = 0.5$ since half of the observations are longer and half are shorter. We calculate the median episode length by solving for t such that $S(t) = 0.5$.

Appropriate Specifications for Multiple Episode Hazard Function Models

The 153,000 episodes in this sample are grouped among the

individuals and hence not independent. As a result, standard errors calculated by conventional regression packages are likely to be underestimated, with t-statistics and significance levels overstated. Allison²¹ and Kelly and Lim²² present good discussions and descriptions of analytical methods of grouping observations.

The general models begin with Cox's proportional hazards model:²³

$$H(t) = \lambda_0(t)e^{x_i\beta} \quad (3)$$

where λ_0 is an unspecified hazard. Andersen and Gill (AG) assume that the risk of an event for a given subject is unaffected by any earlier events that have occurred to the same subject, unless terms that capture such dependence are included explicitly in the model as covariates.²⁴ In contrast, Wei, Lin, and Weissfeld (WLW) allow for dependence among multiple event times, providing efficient pooled estimates of the coefficients and their standard errors.²⁵ Whereas the AG model assumes constant impacts, unless explicitly modeled, the WLW model allows the parameters for an individual's episode 1 to differ from the parameters for episode 2 and so on, with a common effect (and variance) calculated among all of the individual's episodes.

In our application, the observations range from 1 day to 3 years. Episode lengths may be right censored if episodes are either ongoing at the time that data collection starts, or when the data collection effort ends. Failure to account for right censoring will lead to a downward-biased estimate of episode lengths, since we know that episodes are at least as long as those observed.

The discussion above assumes that the researcher knows whether or not a response is censored. We argue that treatment episodes exemplify a class of responses with probabilistic censoring. An episode may begin two weeks before the end of the data collection period. Because all treatment within 30 days of the episode initiation is considered as part of the episode, it is possible, although not certain, that the episode is censored. Assuming that there is no censoring leads to well-known downward biases. However, assuming that *all* of the potentially censored episodes are censored almost certainly biases estimates of episode lengths upward.

This uncertainty is not unique to MH/SA treatment. In the biometrics literature Hougaard²⁶ notes that menopause is defined as the time of the last menstrual bleeding but that it is not possible to say whether an occurrence of bleeding at Time A is the last until a whole lifespan has passed. Operationally, observers wait for one year before determining that menopause occurred at Time A, but Hougaard notes that if a woman dies after a half year without bleeding “it is forever unknown whether she should count as having obtained menopause.” Alternatively the estimated age at which menopause occurs is uncertain. Hougaard does not suggest how to address this uncertainty.

Dropping all potentially censored observations could lead to three serious problems:

- (i) *Loss of information* - Omitting observations sacrifices information. Of the 153,115 episodes, 14,924 or 9.75% are potentially censored. With longer separations (eight weeks or 60 days rather than 30 days), or shorter data windows (one or two years rather than three years), the information loss would be even more severe.
- (ii) *Selection bias* - Omitting observations may result in selection bias by differentially deleting patients with coverage limitations. Also, specific diagnoses (often MH/SA-related) may be selectively deleted, again due to insurance limitations.
- (iii) *Characterizing the distribution* - For treatment episodes, the potential censoring occurs at the beginning or at the end of a calendar year. Because health insurance may limit utilization levels or expenditures by calendar year, utilization and/or costs may be concentrated at the beginning (pent-up demand from the previous year) or at the end (exhausting the year's benefits) of a year. Systematically omitting such episodes will bias estimates of episode length, utilization, and costs downward. This may lead to serious financial consequences for providers and insurers.

After describing the database, we present an estimator to address probable censoring issues, and allow us to use all of the data.

Data

The study population was selected from a large health insurance claims database of 36 self-insured employers, for all treatment events starting January 1, 1989, and ending December 31, 1991. We included claims of all beneficiaries less than 65 years of age (to avoid Medicare overlap) who incurred at least one drug abuse or alcoholism treatment event in the 3-year period. For tractability we limited the database to those subjects with between one and ten episodes in the three-year

period. (Data cells became too small for reliable estimation when more than 10 episodes were used.) This provided 153,115 episodes over 33,998 subjects.

Episodes were classified by their initiating events. Drug abuse episodes were defined by principal International Classification of Disease (ICD-9) diagnoses of 292 (drug psychoses), 304 (drug dependence), or 305.1-305.9 (drug abuse). Alcoholism episodes used diagnoses of 303 (alcohol dependence), 305.0 (alcohol abuse), or 291 (alcohol psychoses). Psychiatric episodes (ICD-9 codes 290, 293-299, 300-302, and 306-319) were similarly identified. The remaining episodes were defined through ICD-9 diagnoses as "surgical" or as "medical." Obstetric-gynecological treatment for women was excluded to facilitate gender comparisons.

Treatment events are classified as either inpatient or outpatient events. Inpatient events consist of all services provided between and including the first and last dates of admissions involving at least an overnight stay. All other services constitute outpatient events. Thus five exclusive diagnostic treatment episode categories (alcoholism, drug, psychiatric, surgical, and medical) are defined at the inpatient and the outpatient levels, for a total of 10 categories.

Table 1 definitions summarizes episode types for each patient by diagnosis and by sequence number (the patient's 1st through 10th episode). Slightly over 14.3% of all episodes (summing the ALC column) are initiated by an alcoholism diagnosis. About 7.8% are initiated by a drug abuse treatment diagnosis, and almost 11.4% are initiated by a psychiatric diagnosis. Approximately 22.2% (row 1) are initial episodes, and over 78.2% of all episodes are accounted for by the first five episodes per subject. In total there are 138,305 outpatient episodes, and 14,810 inpatient episodes.

Goodman, Hankin, Kalist, and Sloan find that characterizing episodes by the initiating event is a valid process, particularly for episodes initiated by inpatient care.²⁷ For inpatient episodes, upwards of 90% of the utilization and costs occur in the same category as the initiating event. Outpatient events are somewhat more heterogeneous, but in episodes initiated by outpatient

Table 1. Fractions of episodes by sequence number

Episode in Sequence	Total	Fraction					Row Sum	Cumulative Row Sum
		ALC	DRG	PSYCH	MED	SURG		
1 (first)	33998	0.0472	0.0282	0.0190	0.1100	0.0176	0.2220	
2 (second)	28459	0.0305	0.0163	0.0196	0.1025	0.0170	0.1859	0.4079
3	23449	0.0211	0.0111	0.0175	0.0895	0.0139	0.1531	0.5611
4	18904	0.0150	0.0076	0.0146	0.0755	0.0108	0.1235	0.6845
5	14898	0.0107	0.0052	0.0121	0.0605	0.0088	0.0973	0.7818
6	11515	0.0073	0.0035	0.0099	0.0477	0.0069	0.0752	0.8570
7	8632	0.0049	0.0023	0.0080	0.0362	0.0049	0.0564	0.9134
8	6230	0.0033	0.0017	0.0060	0.0260	0.0037	0.0407	0.9541
9	4256	0.0021	0.0011	0.0043	0.0177	0.0026	0.0278	0.9819
10	2774	0.0011	0.0006	0.0029	0.0117	0.0018	0.0181	1.0000
Column Sum	153115	0.1432	0.0776	0.1139	0.5774	0.0880		

Table 2. One-day v. multi-day episodes - Variable means

	Total	1-Day	Multi-day
Number	153115	63761	89354
Fraction	1.0000	0.4164	0.5836
Duration	32.5116	1.0000	54.9975
PT_MALE	0.6828	0.6885	0.6787
PT_AGE	36.7794	36.2680	37.1444
PT_HRLY	0.5403	0.5373	0.5424
PT_ACTVE	0.8541	0.8547	0.8537
PT_SELF	0.5886	0.5716	0.6008
EPS_STRO	505.5964	530.2268	488.0207
EPS_DCT	36.8618	18.1130	50.2405
EPS_CPR	0.0870	0.0841	0.0891

drug abuse treatment, for example, over 85% of the costs occur in MH/SA categories.

Table 2 shows the large percentage of one-day episodes. From the second line, 41.6% of the episodes are one-day episodes (a one-day treatment event followed by 31 or more days without treatment). Separate tabulations indicate that only 452 of the 63,761 one-day episodes (0.7%) are inpatient episodes. This means that the remaining 63,309 one-day episodes account for 45.8% of the 138,305 outpatient episodes, a highly skewed distribution whose median is substantially smaller than the mean of 31.55 days. The outpatient mean of 31.55 days and the inpatient mean of 38.61 days differ by only a week, but the outpatient median is far smaller. One would expect this finding because most outpatient care is for acute illnesses.

Men are slightly more likely to have one-day episodes and older subjects are slightly more likely to have multi-day episodes. Insurance deductibles are higher for patients with multi-day episodes (longer episodes mean higher deductibles to be paid), and the copayment rate for multi-day episodes is slightly higher (8.91%, compared to 8.41% for single-day episodes). (All variable definitions are in the **Appendix**).

Database strengths include size, completeness relative to other databases, and accuracy. With the low prevalence of substance abuse treatment, and the stigma of reporting it, population surveys most often provide very small data cells. Clinic-based substance abuse treatment data provide important information on treatment and outcomes at the clinic, but often no information on non-clinic treatment. (Non-clinic treatment includes non-substance abuse treatment, as well as therapy through Alcoholics or Narcotics Anonymous, groups that do not consider themselves to provide medical treatment.) In contrast, we use a large and varied database that examines a host of MH/SA treatments as well as all of the covered treatment for other conditions.

As for weaknesses, the data set cannot identify untreated substance abusers, nor can it identify those with out-of-plan use. It provides treatment information only if services are covered by the insurance plan and are defined with a substance abuse diagnosis code. Like medical records, insurance claims will not specify substance abuse treatment received within the

context of other health care (and thus identified by a non-substance abuse diagnosis code) or community services.

Specifying Models and Interpreting Coefficients

In analyzing episode durations we will compare the AG and the WLW hazard models. We propose the following AG model:

$$\log T_{ikm} = \sum_j \beta_j x_j + \sum_n \delta_n y_n + \sum_g \eta_g f_g + \sum_i \sum_k \sum_m \alpha_{ikm} L_{ikm} + \sum_{v=1}^{v=k} \sum_{u=1}^{u=k} \rho_{uv} z_{uv} \quad (4)$$

T_{ikm} refers to the duration of the i^{th} episode in the sequence, with diagnosis k , at treatment location m . Variables x_j refer to individual level variables including subject's age, gender, and employment status. Variables y_n refer to individual insurance variables, coinsurance and deductible levels. With perfect information and with no variation among employees in the firm, these would be the definitive measures for the individual. Variables f_g characterize the employer where the subject either works or has coverage as the dependent of a worker. One might use employer-specific binary variables to measure differences among employers, but such variables only indicate that different employers are different. Instead we characterize employers with *employer-specific year-specific* (ESYS) measures (based on our population of subjects with either an alcoholism or a drug treatment) such as mean age, mean employment status, or mean percentage male, since employer health care benefits packages may reflect the types of workers that are covered.

We also calculate ESYS mean coinsurance rates and deductibles because employers may offer more than one insurance product, with different copayment rates and different deductibles. The mean may again proxy for employer-specific insurance experience. A second interpretation involves possible errors either in employer policy administration or in data quality. Investigator experience with insurance claims has shown that reported claims may differ from the stated policy. Sometimes these are coding errors; sometimes policies are

simply administered differently for different people. In either case the employer mean may be a better variable than the individual measure. Using both individual and employer measures controls for either possibility.

We explicitly model the episode diagnosis, location, and sequence number with L_{ikm} , and z_{uv} relate the initiating diagnosis of the current episode to the diagnosis of the previous episode. For example, suppose that the patient's current episode is the third episode in the treatment window, that it is initiated by outpatient psychiatric care, and that it follows the second episode, which was initiated by outpatient alcoholism care. Here, variable L_{ikm} is **EPS-3PO** with a value of 1, indicating that the current episode is the third (3) episode in the sequence and is a psychiatric (P) outpatient (O) episode. Variable z_{uv} is **PSY-P-ALC** ("PSYch episode where the Previous episode was an ALCOholism episode") has a value of 1, indicating that the episode preceding the current (psychiatric) episode was an alcoholism episode.

Table 3(a) describes the episode linkages, with the 25 cells summing to the 77.8% of the episodes subsequent to Episode 1 (i.e. the 2nd through 10th episodes). For example 3.46% of all episodes were initiated by alcoholism treatment, immediately preceded by a previous alcoholism treatment episode. Not surprisingly, the largest linkage (0.3276) is for medical treatment, where the immediately preceding treatment was also medical treatment.

Table 3(b) converts **Table 3(a)** into column fractions summing to 1. For example, 36.1% of the alcoholism treatment episodes were immediately preceded by episodes initiated by

alcoholism treatment. Almost 28% of the drug episodes were immediately preceded by drug episodes, and nearly 49% of the psychiatric episodes were immediately preceded by psychiatric episodes.

In contrast to the AG model, the WLW model estimates separate relationships for each of episodes 1 through 10:

$$\begin{aligned} \log T_{ikm} &= \sum_j \beta_{1j} x_j + \sum_g \eta_{1g} f_g + \sum_n \delta_{1n} y_n \\ &\dots \quad \dots \quad \dots \quad \dots \quad \dots \\ \log T_{10,km} &= \sum_j \beta_{10,j} x_j + \sum_g \eta_{10,g} f_g + \sum_n \delta_{10,n} y_n \end{aligned} \quad (5)$$

As with equation (4), T_{ikm} refers to the duration of the i^{th} episode in the sequence, with diagnosis k , at treatment location m . Explanatory variables x_j refer to the subject's age, gender, and employment status, y_n to individual insurance variables, and f_g to the employer. WLW explicitly estimates separate effects for each episode (1 through 10), and provides tests for equality across episodes. However, unlike AG, the WLW formulation does not permit linkage among episodes.

Probable Censoring

Because our database ends December 31, 1991, episodes with events occurring after December 1, 1991 may have right censored lengths since an unobserved event may occur after

Table 3. Linkages for Second Through Tenth Episodes

a. Fractions Linked by Diagnoses					
Previous Episode	Current Episode				
	ALC	DRUG	PSYCH	MED	SURG
ALC	0.0346	0.0025	0.0067	0.0430	0.0079
DRUG	0.0024	0.0137	0.0046	0.0258	0.0041
PSYCH	0.0063	0.0041	0.0463	0.0310	0.0042
MED	0.0449	0.0252	0.0330	0.3276	0.0394
SURG	0.0078	0.0038	0.0042	0.0398	0.0149

b. Column Fractions					
Previous Episode	Current Episode				
	ALC	DRUG	PSYCH	MED	SURG
ALC	0.3607	0.0516	0.0710	0.0921	0.1118
DRUG	0.0250	0.2776	0.0487	0.0553	0.0576
PSYCH	0.0654	0.0822	0.4881	0.0664	0.0591
MED	0.4673	0.5110	0.3474	0.7010	0.5598
SURG	0.0816	0.0775	0.0447	0.0852	0.2117
Sum	1.0000	1.0000	1.0000	1.0000	1.0000

the close of the data collection window, but less than 30 days after the initial event. Similarly, because the database begins on January 1, 1989, any treatment episode *length* starting between January 1 and January 31, 1989 is also potentially right censored (although the *starting dates* are potentially left censored), because the 30-day treatment window may have begun before January 1.

The right censoring is subject to a probability distribution rather than a certainty. Suppose Person 1 had a single event on December 2, 1991 and Person 2 had a single event on December 20, 1991. E_1 is a censored episode only if Person 1 had treatment on January 1, 1992; if he or she had treatment on that date, and there was no further treatment for the next 30 days, then E_1 lasts 30 days. If there was no treatment on January 1, 1992 (even if there was subsequent later treatment), then E_1 was an uncensored episode with a length of 1 day.

E_2 's censoring probability is potentially larger than E_1 since any treatment for Person 2 occurring up to January 19, 1992 would be considered part of episode E_2 . Eleven days have passed (between December 20 and December 31) without an event but it is still possible that an event (which we cannot observe) could occur in the next 20 days. A similar argument with similar logic applies to treatments beginning in the first 30 days of the data window.

Censoring variable c is customarily observed with values of 0 (for right censored observations) or 1 (for uncensored observations). Because we view the censoring variable as a random variable for the possibly censored observations, we cannot estimate either the AG or the WLW models with existing procedures in SAS or in other statistical packages. As a result, new computational methods and estimators are required to handle c and to estimate the model parameters.

Our estimator for median episode length uses comparable episode information to estimate censoring probabilities. Consider, for example, the set of possibly censored episodes that included December 1991. The data available indicate the starting date, the episode length at the last event, and the episode type and location. One may use episodes that included December 1989 (and December 1990) to estimate the probability that an episode with a December event will actually extend into the following month. If 1989, for example, were in fact the last year of the database, then December 1989 episodes extending into 1990 would be censored. A probit model is used predict censoring for 1989 and 1990, and its results then applied to December data for 1991. Goodman et al. discuss alternative estimators in detail.²⁸

Our database contains two relevant types of December 1989 and 1990 episodes.

- (i) *Type O* (ongoing) episodes started before December 1 and were ongoing the date of the last observed event (after December 1), thus possibly censored. We know the episode length on that date. Censoring probabilities for episodes extending into December 1991 that started prior to December 1, 1991, will be predicted by probit regressions for 1989 and 1990 *Type O* episodes.

$$Pr(cens) = \theta_0 + \theta_1 * Ep. Length (as of 12/1) + \theta_2 * Ep. Location (inpatient or outpatient) + \sum_{type=1}^k \theta_{3k} Treatment_k . \quad (6a)$$

- (ii) *Type A* (after) episodes started after December 1. Since this *starting date* was within 30 days of the probable censoring date, these episodes were possibly censored. As with the *Type O* episodes, we know how long these episodes lasted, but we do not know the sequencing of the events. Censoring probabilities for December 1991 episodes that started after December 1, 1991 will be predicted by probit regressions for 1989 and 1990 *Type A* episodes.

$$Pr(cens) = \gamma_0 + \gamma_1 * Start date + \gamma_2 * Ep. Location (inpatient or outpatient) + \sum_{type=1}^k \gamma_{3k} Treatment_k . \quad (6b)$$

The alternative estimator for episodes starting within the *first* 30 days of the data window (January 1 through January 30, 1989) is analogous. We use January 1990 and January 1991 episodes to generate censoring probabilities for January 1989.

Equations (6a) and (6b) assign each potentially censored observation a probabilistic value (either 0 or 1) for the censoring indicator c . The relevant censoring adjustment is made if 0 is assigned, and the hazard function is estimated conditional on the draw. Over a repeated set of drawings, individual observations will approach their asymptotic probability of being censored. We will adjust the median episode lengths based on these probabilities.

Results

This section presents estimation results. **Table 4** examines the hazard function estimates using the AG specification and **Table 5** the WLW specification. The two specifications are then compared. **Table 6** shows the probit censoring adjustments. Subsequent analyses and accompanying figures address the estimates of episode lengths after adjusting for probable censoring.

AG Estimators

Table 4 presents the AG analysis. The five sets of variables grouped together are: (i) individual; (ii) insurance; (iii) employer-specific year-specific (ESYS); (iv) binary, relating to episode type and sequence; and (v) linkage.

For the same employer, men's episodes had an 11.6% (or $e^{0.1102}$) higher hazard than women's episodes, meaning they were likely to be shorter. The negative hazard for age suggests slightly longer episodes for older subjects. Active workers (those currently employed) had slightly longer episodes (negative hazard), as did primary beneficiaries (measured by PT_SELF). The later the episode started (EPS_STR0), the shorter it was likely to be.

It is instructive to examine the individual and the employer variables jointly. As noted above, for the same employer, men's

Table 4. Multiple episode durations - AG Estimator

Variable	Coefficient	Std. Error	t-stat	Variable	Coefficient	Std. Error	t-stat
Individual				EPS_4MO	-0.0767	0.0249	-3.08
PT_MALE	0.1102	0.0064	17.15	EPS_4PI	-0.9230	0.0868	-10.63
PT_AGE	-0.0028	0.0002	-11.50	EPS_4PO	-0.5756	0.0408	-14.12
PT_HRLY	-0.0003	0.0071	-0.04	EPS_4SI	-0.3045	0.1181	-2.58
PT_ACTVE	-0.0262	0.0091	-2.87	EPS_4SO	0.0527	0.0389	1.35
PT_SELF	-0.0637	0.0067	-9.51	EPS_5AI	-0.7604	0.0621	-12.26
EPS_STR0	0.0006	0.0000	48.80	EPS_5AO	-0.4989	0.0451	-11.07
Insurance				EPS_5DI	-0.6461	0.0801	-8.07
EPS_DCT	-0.0043	0.0000	-97.13	EPS_5DO	-0.3824	0.0608	-6.29
EPS_CPR	-0.0036	0.0295	-0.12	EPS_5MI	-0.2008	0.1121	-1.79
Employer				EPS_5MO	0.0006	0.0251	0.02
MALE_AVG	0.1264	0.0809	1.56	EPS_5PI	-0.7105	0.0991	-7.17
AGE_AVG	-0.0010	0.0013	-0.79	EPS_5PO	-0.4200	0.0421	-9.97
HRLY_AVG	0.1615	0.0148	10.93	EPS_5SI	-0.6835	0.1536	-4.45
ACTV_AVG	-0.1302	0.0207	-6.28	EPS_5SO	0.0768	0.0408	1.88
SELF_AVG	-0.4878	0.0473	-10.31	EPS_6A	-0.5639	0.0461	-12.23
DCT_AVG	0.0049	0.0002	25.65	EPS_6D	-0.4386	0.0622	-7.05
CPR_AVG	-0.2337	0.0820	-2.85	EPS_6P	-0.3529	0.0435	-8.12
Type and Sequence				EPS_6S	0.0581	0.0427	1.36
EPS_1AI	-1.3651	0.0322	-42.41	EPS_6M	-0.0104	0.0256	-0.40
EPS_1AO	-1.4057	0.0313	-44.97	EPS_7A	-0.5003	0.0508	-9.84
EPS_1DI	-1.3864	0.0352	-39.42	EPS_7D	-0.4009	0.0697	-5.75
EPS_1DO	-1.4611	0.0354	-41.27	EPS_7P	-0.3268	0.0452	-7.23
EPS_1MI	-1.2254	0.0679	-18.05	EPS_7S	0.0943	0.0471	2.00
EPS_1MO	-1.2215	0.0278	-43.91	EPS_7M	0.0532	0.0265	2.01
EPS_1PI	-1.5723	0.0589	-26.71	EPS_8A	-0.4311	0.0588	-7.34
EPS_1PO	-1.9120	0.0373	-51.21	EPS_8D	-0.2757	0.0773	-3.57
EPS_1SI	-1.4812	0.0992	-14.93	EPS_8P	-0.3238	0.0490	-6.60
EPS_1SO	-1.1248	0.0347	-32.38	EPS_8S	0.1764	0.0527	3.35
EPS_2AI	-1.0210	0.0423	-24.14	EPS_8M	0.0798	0.0280	2.85
EPS_2AO	-0.7891	0.0387	-20.40	EPS_9A	-0.3542	0.0695	-5.09
EPS_2DI	-0.9961	0.0527	-18.90	EPS_9D	-0.2244	0.0955	-2.35
EPS_2DO	-0.6985	0.0497	-14.07	EPS_9P	-0.2351	0.0541	-4.35
EPS_2MI	-0.5738	0.0706	-8.13	EPS_9S	0.1932	0.0618	3.13
EPS_2MO	-0.3936	0.0252	-15.62	EPS_9M	0.1284	0.0306	4.20
EPS_2PI	-1.1198	0.0666	-16.82	Linkage			
EPS_2PO	-0.8689	0.0397	-21.89	ALC_P_ALC	0.2366	0.0312	7.58
EPS_2SI	-0.6467	0.0988	-6.55	ALC_P_DRG	0.1959	0.0605	3.24
EPS_2SO	-0.2541	0.0362	-7.03	ALC_P_PSY	0.1261	0.0434	2.91
EPS_3AI	-0.9062	0.0479	-18.94	ALC_P_MED	-0.0085	0.0300	-0.28
EPS_3AO	-0.6882	0.0401	-17.16	DRG_P_ALC	0.1681	0.0645	2.61
EPS_3DI	-0.8615	0.0618	-13.95	DRG_P_DRG	0.0760	0.0446	1.70
EPS_3DO	-0.5541	0.0517	-10.72	DRG_P_PSY	-0.0032	0.0565	-0.06
EPS_3MI	-0.3828	0.0811	-4.72	DRG_P_MED	0.0062	0.0415	0.15
EPS_3MO	-0.1937	0.0249	-7.79	PSY_P_ALC	0.1149	0.0456	2.52
EPS_3PI	-1.0001	0.0724	-13.81	PSY_P_DRG	0.0774	0.0506	1.53
EPS_3PO	-0.6970	0.0400	-17.42	PSY_P_PSY	0.1479	0.0342	4.32
EPS_3SI	-0.4668	0.1104	-4.23	PSY_P_MED	-0.0785	0.0353	-2.23
EPS_3SO	-0.0656	0.0371	-1.77	MED_P_ALC	0.2804	0.0180	15.57
EPS_4AI	-0.8251	0.0532	-15.50	MED_P_DRG	0.3173	0.0207	15.32
EPS_4AO	-0.5871	0.0424	-13.84	MED_P_PSY	-0.0253	0.0197	-1.28
EPS_4DI	-0.7282	0.0703	-10.36	MED_P_MED	0.0217	0.0135	1.61
EPS_4DO	-0.4621	0.0562	-8.22	SRG_P_ALC	0.1654	0.0365	4.54
EPS_4MI	-0.4374	0.0898	-4.87	SRG_P_DRG	0.1320	0.0462	2.86
				SRG_P_PSY	-0.0892	0.0458	-1.95
				SRG_P_MED	-0.0984	0.0245	-4.01

episodes had an 11.6% higher hazard than women's episodes. At the employer level, the higher the percentage men (MALE_AVG), the shorter still the episode. Comparing an employer for which 60% of those covered were male with one with 50% coverage, the hazard was 1.26% (that is, $e^{(0.6 - 0.5) \times 0.1264}$) higher. Although hourly and non-hourly individual workers' episodes were not significantly different at the individual level, subjects with employers having higher proportions of covered hourly workers (HRLY_AVG) had significantly shorter episodes.

Insurance variables also demonstrated both individual and employer effects. Holding employer constant, subjects with higher deductibles had longer episodes, but individual coinsurance rates were insignificant. However subjects working at employers with higher deductibles had shorter episodes. One obtains the joint impact by adding the deductible coefficients for EPS_DCT and DCT_AV = $-0.0043 + 0.0049 = 0.00053$. A 100 dollar deductible increase for all individuals at a given employer was related to a 5.4% increase in the hazard (and a decrease in episode length).

The individual coinsurance rate was not statistically significant, but the employer coinsurance rate was. The joint impact of EPS_CPR and CPR_AV = $-0.0036 - 0.2337 = -0.2373$, suggesting that an increase in the coinsurance rate from 0.05 to 0.10 decreased the hazard by approximately 1.2% (the product of 0.05 and coefficient -0.2373).

The binary episode type and sequence descriptors provide useful insights into the sequential nature of the episodes. We characterize the first 5 episodes by both inpatient/outpatient status and by diagnosis type. A comparison of the binary terms indicates the impact of the specific diagnosis/ location pair on the hazard. For Episode 1, episodes initiated by surgical/outpatient care have the largest coefficient (-1.1248), indicating the shortest duration; episodes initiated by psychiatric/outpatient care have the smallest Episode 1 coefficient (-1.9120), indicating a significantly lower hazard, and hence longer duration, suggesting a sequence of events.

The linkage variables add depth to the analyses. Consider an alcoholism treatment episode immediately preceded by another alcoholism episode (ALC_P_ALC). The coefficient of 0.2366 implies a greater hazard than if this alcoholism episode had been immediately preceded by a medical episode (ALC_P_MED) with a coefficient of -0.0085 . In contrast, consider a drug treatment episode preceded by another drug episode. Variable DRG_P_DRG (coefficient of 0.0760) shows that a repeat drug episode is likely to be longer (lower hazard) than a repeat alcoholism episode (ALC_P_ALC coefficient of 0.2366). A general perusal of these linkages indicates that following either a drug or an alcoholism event implied a slightly higher hazard (increased probability of ending and hence shorter episode) than the omitted category (following surgery).

WLW Estimators

We estimate 10 hazard functions with the WLW method - one for each episode in the sequence. The common hazard, a weighted average of the episode-specific hazards, can be compared to the AG hazards in order of magnitude, and

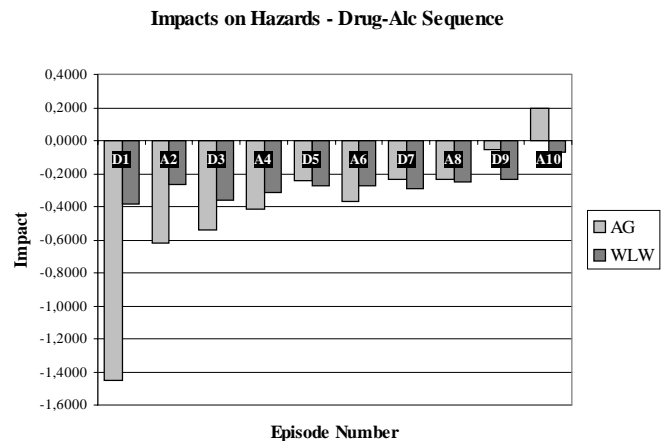


Figure 1. Hazards of Drug - Alcoholism Sequence

significance. One can also test (using F -tests) whether the covariates have constant impacts across the sequence. Men, for example, have higher hazards than women for all episodes, but significantly higher for earlier ones than for later ones.

For some variables, impacts differ both quantitatively and qualitatively depending on where in the sequence they occur. Episode starting date EPS_STR0 is a prime example. For early episodes later starting dates imply higher hazards (shorter episodes); for later episodes (Episodes 5 through 10), later starting dates imply lower hazards (longer episodes). The common effect is positive (because there are greater numbers of Episodes 1 through 3 than Episodes 5 through 10 contributing to the weighted common effect), but the event-specific coefficients are significantly different.

The coefficients for alcoholism, drug, and psychiatric hazards are all significantly negative, indicating smaller hazards (longer episodes) than the omitted surgery category. Looking at **Table 5**, the alcoholism treatment coefficient is lowest (-0.3440) in Episode 1, indicating the longest episode, and highest in Episode 10 (-0.0338). The weighted mean of -0.2756 differs significantly from 0; the F -test rejects coefficient equality over the 10 episodes. The drug and psychiatric treatment coefficients have similar patterns, weighted means, and F -statistics.

Comparing AG and WLW Estimators

There is no direct way to compare the AG and the WLW methods, but we propose to examine the differences by calculating the hazards of specific sequences of events. **Figure 1** investigates a stylized set of events in which drug episodes (1, 3, 5, 7, and 9) alternate with alcoholism episodes (2, 4, 6, 8, and 10). The WLW relative hazards are read directly from the episode-specific estimates in **Table 5**. Assuming that 10% of the episodes are inpatient and 90% are outpatient; the hazards vary from -0.38 (Episode 1) to -0.07 (Episode 10). The AG relative hazards, using the *type and sequence* variables and the *linkage* variables (and assuming the same proportions inpatient and outpatient) show considerably more variation, from -1.45 (Episode 1) to $+0.19$ (Episode 10).

Table 5. Multiple episodes hazards - WLW Estimator

Variable	Episode Number									
	1	2	3	4	5	6	7	8	9	10
PT_MALE	0.1793*	0.1640*	0.1372*	0.1287*	0.1229*	0.0923*	0.1170*	0.1266*	0.0876*	0.1535*
PT_AGE	-0.0045*	-0.0038*	-0.0034*	-0.0050*	-0.0033*	-0.0036*	-0.0030*	-0.0017	-0.0045*	-0.0019
PT_HRLY	0.0176	0.0248	0.0106	0.0186	-0.0060	0.0442	0.0277	-0.0342	0.0225	0.0792
PT_SELF	-0.0460*	-0.0720*	-0.0589*	-0.0552*	-0.0462*	-0.0553*	-0.0628*	-0.0689*	-0.0084	-0.0506
EPS_LOC	-0.0502*	-0.1874*	-0.1540*	-0.1674*	-0.1697*	-0.2290*	-0.2234*	-0.3311*	-0.3568*	-0.3780*
EPS_STR0	0.0012*	0.0001*	0.0001*	0.0000	-0.0002*	-0.0003*	-0.0003*	-0.0006*	-0.0010*	-0.0014*
EPS_DCT	-0.0032*	-0.0034*	-0.0039*	-0.0037*	-0.0041*	-0.0041*	-0.0036*	-0.0027*	-0.0042*	-0.0034*
EPS_CPR	-0.8110*	-0.2223*	0.0746	-0.0676	0.1770*	0.0400	0.2124	0.3462*	0.6237*	0.9127*
ALC	-0.3440*	-0.2489*	-0.3165*	-0.2995*	-0.2401*	-0.2491*	-0.2229*	-0.2181*	-0.1627*	-0.0338
DRG	-0.3770*	-0.2803*	-0.3322*	-0.2923*	-0.2392*	-0.2307*	-0.2421*	-0.1189	-0.1610*	-0.0554
PSY	-0.7844*	-0.5033*	-0.5262*	-0.4849*	-0.3858*	-0.3481*	-0.3016*	-0.3186*	-0.3356*	-0.1429
MED	-0.0648*	-0.0089	-0.0411	-0.0240	0.0391	-0.0156	0.0198	0.0130	0.0106	0.0658
MALE_AVG	-0.1649	-0.0275	0.2715	0.0783	0.3907	0.1550	0.1972	0.3823	0.3478	0.9755
AGE_AVG	-0.0189*	0.0021	0.0036	0.0075*	0.0136*	0.0075	0.0104	0.0119	0.0194	0.0238
HRLY_AVG	0.3380*	0.1528*	0.1312*	0.0269	0.0575	-0.0376	0.0043	0.0891	0.0458	-0.0247
ACT_AVG	-0.4355*	-0.0519	-0.1601*	-0.0249	-0.0528	0.0320	0.0284	0.1384	-0.2050	0.2771
SELF_AVG	-0.5899*	-0.4732*	-0.6749*	-0.4098*	-0.6709*	-0.2768*	-0.2206*	-0.5669*	-0.5486	-0.6368
DED_AVG	0.0061*	0.0031*	0.0030*	0.0026*	0.0031*	0.0026*	0.0024*	0.0004	0.0006	-0.0003
CPR_AVG	0.4750*	0.3088	0.2777	0.0144	-0.2492	-0.4648	-0.4052	0.0189	0.0301	-0.3845

* Significant at 5% level.

Table 5. Multiple episodes hazards - WLW Estimator (cont.)

Variable	Common Coefficient	Standard Error	t-stat	Equal Coeffs?	Joint Effect?
PT_MALE	0.1404	0.0074	19.03	No	Yes
PT_AGE	-0.0037	0.0003	-14.11	Yes	Yes
PT_HRLY	0.0172	0.0078	2.21	Yes	No
PT_SELF	-0.0565	0.0077	-7.32	Yes	Yes
EPS_LOC	-0.1518	0.0086	-17.67	No	Yes
EPS_STR0	0.0002	0.0000	19.38	No	Yes
EPS_DCT	-0.0036	0.0001	-63.84	No	Yes
EPS_CPR	-0.1159	0.0303	-3.82	No	Yes
ALC	-0.2756	0.0116	-23.80	No	Yes
DRG	-0.2904	0.0134	-21.62	No	Yes
PSY	-0.4834	0.0124	-39.07	No	Yes
MED	-0.0155	0.0096	-1.62	Yes	No
MALE_AVG	0.0849	0.0891	0.95	Yes	No
AGE_AVG	0.0011	0.0014	0.79	Yes	Yes
HRLY_AVG	0.1104	0.0161	6.86	No	Yes
ACT_AVG	-0.1254	0.0189	-6.63	No	Yes
SELF_AVG	-0.5260	0.0534	-9.85	Yes	Yes
DED_AVG	0.0034	0.0002	16.13	No	Yes
CPR_AVG	0.1500	0.0910	1.65	Yes	No

Impacts on Hazards - Drug Sequence

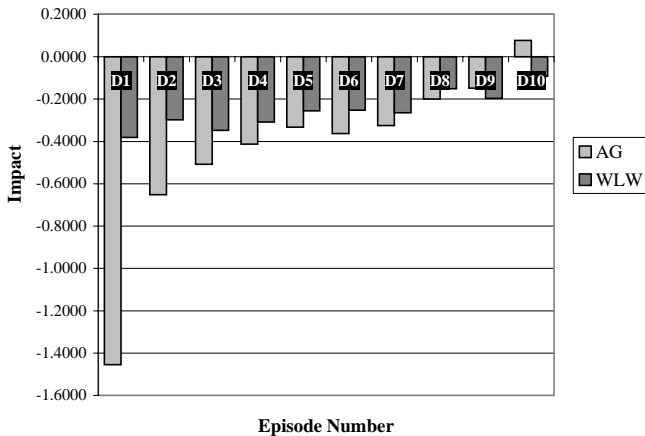


Figure 2. Hazards of Drug Sequence

Figure 2 considers a stylized set of 10 consecutive drug episodes. Once again, there is considerably more variation in the hazards with the AG estimator than with the WLW estimator.

What accounts for the difference? The WLW model computes the episode-specific hazards (and hence the survival rates) directly. It also estimates the coefficients and the within-subject correlation more directly than does the AG method. However, the AG method allows the researcher to link

characteristics of preceding and succeeding episodes explicitly, an option that is not available with WLW. Also, even with a fast personal computer with substantial storage (27 GB) and memory (384 MB), some variables had to be omitted from the WLW analysis. The model presented has 190 coefficients (19 variables over 10 events). Efforts to add further coefficients were not successful.

Probit Censoring Adjustments

Table 6 displays the probit censoring adjustments discussed earlier. All were estimated with two years of data. For ongoing December 1 episodes (**Table 6a**) estimated with 1989 and 1990 data, the positive coefficient on EPS_LENGTH (0.0027) indicates that episodes of greater length on December 1 are more likely to extend past December 31. This implies censoring when the probit equation is applied to possibly censored 1991 observations. Inpatient episodes, with a coefficient on EPS_LOC of -0.2661, are less likely to imply censoring. ALC, DRUG, PSYCH, or MED are all more likely to imply censoring than the omitted surgery category.

For the *Type A - December* adjustment (**Table 6b**), again estimated for 1989 and 1990, the coefficient of 0.0303 for episode starting date (START) implies that the later in December the episode starts, the more likely that it will extend past December 31. Inpatient episodes are more likely to imply censoring. Again, ALC, DRUG, PSYCH, or MED are more

Table 6 - Probit estimate of censoring probabilities

a. Ongoing Episodes - Type O

Variable	Type O - December		Type O - January	
	Coefficient	Std. Error	Coefficient	Std. Error
INTERCEPT	-0.2771	0.0508*	-0.2561	0.0520*
EPS_LENGTH	0.0027	0.0001*	0.0028	0.0001*
EPS_LOC	-0.2661	0.0474*	-0.0424	0.0456
ALC	0.2698	0.0615*	-0.1302	0.0609*
DRUG	0.2401	0.0710*	-0.1708	0.0686*
PSYCH	0.3852	0.0594*	-0.0040	0.0585
MED	0.1417	0.0535*	0.0078	0.0544

b. Episodes Starting after December 1 or before January 31 - Type A

Variable	Type A - December		Type A - January	
	Coefficient	Std. Error	Coefficient	Std. Error
INTERCEPT	-10.9882	0.6391*	0.0263	0.0553
START	0.0303	0.0018*	-0.0320	0.0016*
EPS_LOC	0.5532	0.0617*	0.7002	0.0560*
ALC	0.4457	0.0667*	0.1676	0.0630*
DRUG	0.4893	0.0777*	0.0993	0.0713
PSYCH	0.5564	0.0674*	0.1706	0.0638*
MED	0.0316	0.0533	-0.0151	0.0530

* indicates 5% significance

Median Episode Length

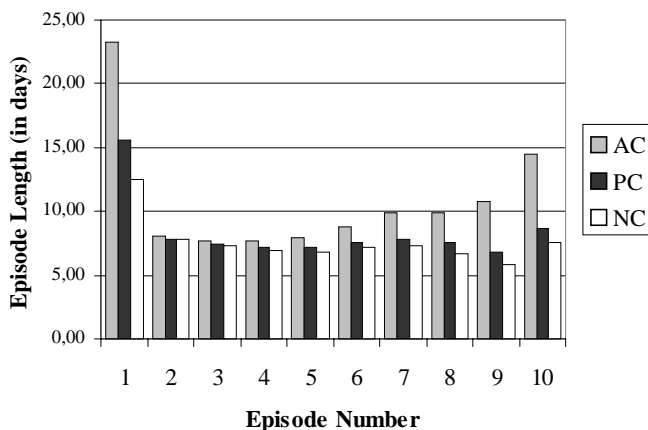


Figure 3. Differences in Medians - All-censored, probably censored, and uncensored

likely imply censoring than the omitted surgery category.

The January adjustments estimated for 1990 and 1991, to be applied to episodes starting in January 1989, are qualitatively similar. The *Type O - January* adjustment implies that the longer the current episode lasts after January 31, the more likely that it will have started before January 1, implying censoring. The *Type A - January* adjustment, with a negative start date coefficient, indicates that the later in January the episode started, the less likely that it will have started before January 1. Note that the coefficients of the start dates for both Type A adjustments are similar in absolute impacts (0.0303 for December; -0.0320 for January). This implies that the closer the start date to the last (for December) or first (for January) day of the window, the more likely it will either extend past December 31, or start before January 1. When applied to the possibly censored episodes, this increased likelihood implies more probable censoring.

Survival Functions and Median Episode Lengths

Thus far we have estimated the covariates of episode length, but we have not addressed the estimated median length. Failure to adjust for potential censoring implies that episode length, utilization, and costs are as measured; however if episode censoring occurs, this must imply increased utilization (which lengthens the episode) and increased costs. Assuming that any potentially censored episode is in fact censored, almost certainly overadjusts for the potential censoring.

This section presents WLW survival functions for the cases of: (1) no censoring NC; (2) probable censoring PC; and (3) all censoring AC. While AC estimates will be higher than the NC estimates (with the PC estimates in between) the magnitudes of the differences, and their distributions over the different episodes (1st through 10th) in the sequence, are not apparent. Since the WLW estimator provides separate estimators for each of the 10 episodes in the sequence, it is the easier of the two methods to use for estimating the medians.

Figure 3 demonstrates the substantial differences. The median episode length for the Episode 1 is longer than for all

other episodes with the NC median length slightly over 12 days. Assuming that all potentially censored episodes are censored provides an AC median length of almost 24 days. The PC estimator gives a median of slightly more than 15 days, indicating that the AC method overadjusts for probable censoring by 9 days.

There is less variation among the three estimators for Episodes 2 through 5. Because these episodes must occur after the first 30 days, they are less likely to be censored. For Episode 4, the AC, PC, and NC estimated medians of 7.7, 7.2, and 7.0 (respectively) vary by less than one day. Moving toward Episode 10 (the end of the three-year window), the censoring probabilities increase, and so do the differences among the AC (14.5 days), PC (8.5 days), and NC (7.6 days) estimators.

Figure 3 demonstrates several key points. Different episodes in the sequence have different median lengths. Second, censoring adjustments are necessary; otherwise episode length estimates are biased downward. Third, assuming that all potentially censored episodes *are* censored, overestimates the median length, and by inference utilization and cost. Adjusting for probable censoring tempers these upward-biased adjustments.

Discussion and Conclusions

This article characterizes multiple health treatment episodes for a sample of 33,998 insured clients with at least one alcohol or drug treatment diagnosis between January 1, 1989 and December 31, 1991, using proportional hazard models. We address (i) determinants of episode length, (ii) methods for examining individuals' multiple episodes, and (iii) the impacts of probable censoring on estimated lengths.

- (i) *Determinants of episode length.* We identify both individual and employer effects on episode length. We find that episodes vary in length by coinsurance rate, insurance deductible, diagnosis type, and treatment location (inpatient or outpatient). Further, we show that episode lengths may depend on the treatments that occurred in previous episodes.
- (ii) *Multiple episodes.* Multiple episodes require special statistical methods because the individual observations are not independent. Both the AG and the WLW models have merit. The AG model appears to permit more flexibility in estimating hazards, and allows researchers to model impacts of prior diagnoses on future episodes. The WLW model provides a convenient way to examine impacts of sociodemographic variables across episodes. It also provides efficient pooled estimates of coefficients and their standard errors.
- (iii) *Probable censoring.* Probable censoring arises because the very nature of health care treatment episodes allows for some time to elapse between observed events. If the observation window closes before the appropriate period of time lapses, the duration may be censored. Just as ignoring the censoring problem results in estimated lengths (implying treatment utilization and costs) that are too low, assuming that all of the potentially censored observations are censored,

leads to lengths that are too high. We provide a method that adjusts the medians appropriately according to the probability of censoring.

The methods developed here are important in analyzing MH/SA treatment episodes, and can be applied to a wide range of health services research in which censoring is probabilistic rather than certain. Unless the last observed treatment event corresponds to the last day of the data collection period, it is uncertain whether episodes are truly censored and whether estimates of costs or utilization are accurate. We propose a method that addresses these censoring issues and we provide an estimator that is easy for analysts and practitioners to use.

Appendix. Variable Definitions

Tables 1-5

PT_MALE - 1 if patient is male; 0 otherwise
 PT_AGE - patient age in years
 PT_HRLY - 1 if the patient is an hourly employee; 0 otherwise
 PT_ACTVE - 1 if the patient is currently employed; 0 otherwise
 PT_SELF - 1 if the patient is the primary beneficiary; 0 otherwise
 EPS_LOC - 1 if inpatient; 0 otherwise
 EPS_STR0 - starting date of episode (January 1, 1989 = 1; December 31, 1991 = 1065)
 EPS_CPR - episode coinsurance rate (0 = no out-of-pocket; 1 = full)
 EPS_DCT - episode deductible in dollars
 MALE_AVG - employer (year-specific) mean of covered employees who are male
 AGE_AVG - employer (year-specific) mean age of covered employees
 HRLY_AVG - employer (year-specific) mean of hourly employees
 ACTV_AVG - employer (year-specific) mean of currently employed subjects
 SELF_AVG - employer (year-specific) mean of employees who are primary beneficiaries
 CPR_AVG - employer (year-specific) mean of coinsurance rate
 DCT_AVG - employer (year-specific) mean deductible payment
 ALC - 1 if initiating event was alcoholism treatment; 0 otherwise
 DRUG - 1 if initiating event was drug treatment; 0 otherwise
 PSYCH - 1 if initiating event was psychiatric treatment; 0 otherwise
 MED - 1 if initiating event was medical treatment; 0 otherwise
 ALC - 1 if initiating event was alcoholism treatment; 0 otherwise
 TYP_AVG - employer (year-specific) mean of inpatient v. outpatient episode
 EPS_ikm - 1 if episode is of sequence i , diagnosis k , at location m ; 0 otherwise $i = 1, 10$; $k = \text{ALC, DRG, PSYCH, MED, SURG}$; $m = \text{inpatient, outpatient}$
 u_P_v - 1 if episode is of type u , and previous episode was of type v ; 0 otherwise $u, v = \text{ALC, DRG, PSYCH, MED, SURG}$

Table 6

START - episode start date (January 1 = 1; December 31 = 365)
 EPS_LENGTH - length of Type O episode in days on December 1 (January 31)
 EPS_LOC - 1 if inpatient; 0 otherwise
 ALC - 1 if initiating event was alcoholism treatment; 0 otherwise
 DRUG - 1 if initiating event was drug treatment; 0 otherwise
 PSYCH - 1 if initiating event was psychiatric treatment; 0 otherwise
 MED - 1 if initiating event was medical treatment; 0 otherwise

Acknowledgments

We thank Thomas McLellan for his advice and technical expertise. The findings are ours and do not represent NIDA, the Blue Cross Blue Shield Foundation, or Wayne State University.

References

- Frank R, McGuire T. Estimating costs of mental health and substance abuse coverage. *Health Affairs* 1995; **14**: 102-115.
- Mechanic D, Schlesinger M, McAlpine DD. Management of mental health and substance abuse services: State of the art and early results. *Milbank Q* 1995; **73**: 19-55.
- Greene, SB, Gungelman DL. The conversion of claims files to an episode data base: A tool for management and research. *Inquiry - J Health Care* 1984; **21**: 189-94.
- Levy ST, Ninan PT (Eds). *Schizophrenia: Treatment of Acute Psychotic Episodes*. Washington: American Psychiatric Press, 1989.
- Buczko W. Inpatient transfer episodes among aged Medicare beneficiaries. *Health Care Financ Rev* 1993; **15**: 71-87.
- Haas-Wilson D, Cheadle A, Scheffler R. Demand for mental health services: An episode of treatment approach. *Southern Econ J* 1989; **56**: 219-32.
- Solon JA, Feeney JJ, Jones SH, et al. Delineating episodes of medical care. *Am J Public Health* 1967; **57**: 401-408.
- Ball JK, Roskamp J. General methods for diagnosis- and service-specific analyses. *Med Care* 1986; **24**: S7-S17.
- Keeler EB, Rolph JE. The demand for episodes of treatment in the Health Insurance Experiment. *J Health Econ* 1988; **7**: 337-367.
- Keeler EB, Manning WG Jr., Wells KB. The demand for episodes of mental health services. *J Health Econ* 1988; **7**: 369-392.
- Newhouse JP and the Insurance Experiment Group. *Free for All: Lessons from the Rand Health Insurance Experiment*. Cambridge, MA: Harvard University Press, 1993.
- Wells, KB, Keeler E, Manning W G Jr. Patterns of outpatient mental health care over time: Some implications for estimates of demand and for benefit design. *Health Serv Res* 1990; **24**: 773-790.
- Hornbrook MC, Hurtado AV, Johnson RE. Health care episodes: Definition, measurement, and use. *Med Care Rev* 1985; **42**: 163-218.
- Moscovice I. A method for analyzing resource use in ambulatory care settings. *Med Care* 1977; **15**: 1024-1044.
- Cave DG. Profiling physician practice patterns using diagnostic episode clusters. *Med Care* 1995; **33**: 463-486.
- Kessler LG, Steinwachs DM, Hankin JR. Episodes of psychiatric utilization. *Med Care* 1980; **18**: 1219-1227.
- Reynolds, CF, Frank E, Perel JM, et al.. Treatment of consecutive episodes of major depression in the elderly. *Am J Psychiatry* 1994; **151**: 1740-3.
- Branch, LG, Goldberg HB, Choh VA, Williams J. Medicare home health: A description of total episodes of care. *Health Care Financ Rev* 1993; **14**: 59-74.
- Holmes, AM, Deb P. Provider choice and use of mental health care: Implications for gatekeeper models. *Health Serv Res* 1998; **13**: 1263-1284.
- Berndt ER, Busch SH, Frank RG. *Price indexes for acute phase treatment of depression*. National Bureau of Economic Research, Working Paper 6799, November 1998.
- Allison, PD. *Survival Analysis Using the SAS System: A Practical Guide*. Cary NC: SAS Institute Inc., 1995.
- Kelly PJ, Lim L L-Y. Survival analysis for recurrent event data: An Application to Childhood Infectious Diseases. *Stat Med* 2000; **19**: 13-33.
- Cox, DR. Regression models and life tables. *J Roy Stat Soc* 1972; **B34**: 187-220.
- Andersen PK, Gill RD. Cox's regression model for counting processes: A large sample study. *Ann Stat* 1982; **10**: 1100-1120.
- Wei LJ, Lin DY, Weissfeld L. Regression analysis of multivariate incomplete failure time data by modeling marginal distributions. *J Am Stat Assoc* 1989; **84**: 1065-1073.
- Hougaard P. Fundamentals of survival data. *Biometrics* 1999; **55**: 13-22.
- Goodman AC, Hankin JR, Kalist DE, Sloan JJ. *Episode profiles for substance abusers: What do episodes look like?* Wayne State University, November 2000.
- Goodman, AC, Hankin JR, Kalist DE, Peng Y, Spurr SJ. *Estimating episode lengths when some observations are probably censored*. Wayne State University, July 2001.